

**Presenter:** Dr. Brian Helmke, Associate Professor, Department of Biomedical Engineering, University of Virginia

**Topic:** ASEE Education Showcase Deep Dive: Stomp Rockets, Tennis Balls, and Conservation of Momentum - ASEE Education Showcase Deep Dive

**Resources:**

**Discussion and Lecture Notes:**

Lecture Notes:

- Biotransport required core class with ~70 students
- Students have heard “it’s hard”, “it’s complicated”, etc.
- Difficult concept to understand is the idea behind conservation of momentum
- Mass conservation and keep track of mass flows in and out of a container, but keeping track of momentum flowing is hard
- Newton’s 2<sup>nd</sup> law and conservation of momentum
- Stomp Rockets + Tennis Balls
  - Stomp Rockets is a toy where you set up a rocket with a tripod, aim it, and the use an air pocket that you stomp on and the rocket goes flying by creating a pulse of air that begins at the cushion
  - Why does the rocket go flying?
    - Air pushing the rocket, air is exerting a force on the rocket
    - If you exert a force on an object, it accelerates
    - Newton’s law: Force = mass\*acceleration
  - Tennis Ball:
    - Drop tennis balls, it falls because gravity causes it to fall
    - What happens to the ball as it falls?
      - It accelerates. The force of gravity is causing it to accelerate as it falls to the floor
  - Momentum:
    - Equation:  $P = \text{momentum} = \text{mass} * \text{velocity}$
    - The velocity of the ball and stomp rocket are increasing because of a force
    - We can say the momentum of the ball or stomp rocket are increasing due to a force
    - There is a relationship between the rate of change of momentum and the force applied to the object
    - Write it down as a rate of change of momentum with relation to its force applied
    - $P = mv$  or  $dp/dt = d/dt (mv)$
    - $dp/dt = m dv/dt = ma = F = \text{rate of change of momentum is equivalent to a force}$
    - Rate of change of momentum *results* from an applied force
  - Throw ball against a wall
    - Assume it bounces off the wall and comes back at the same speed. Is the velocity constant?
      - No because it changed direction, velocity is a vector
      - Is momentum constant when it bounces off a wall?
      - A rate of change in momentum occurs because of a force acting on the wall. It still works because the momentum changes because the wall is exerting a force on the ball.
      - The ball is accelerating by the force acting on the ball when it bounces off the wall
      - So velocity is changes as acceleration is changing *direction*
    - The ball accelerates because it changed *direction* or it can change in *time*
  - Change of momentum in *space* and *time*
    - So the diff eq is now:  $\rho (dv/dt) + \rho v \cdot \dot{\Delta} v = \sum F$

- Where we sum the *temporal acceleration* and the *spatial acceleration* of rate of change of momentum is equal to the sum of forces
- Goal of activity is to connect messy 3d vector equations with partial derivatives to an intuitive thought like mass \* acceleration.

Discussion:

- Did you see a better understanding of the concept on an exam? Did you compare with and without the example?
  - Have not done this but they mention it allows them to connect and remember back to the lecture
  - Discuss example of tubes at a t-junction, water with forces at an angle
- How do you provide enough examples for biological processes and which book would you use?
  - I don't send them to a specific book, so one strategy is to use physical examples and then send them out to find a force example with fluids and how it changes to the momentum of the fluid.
  - Example: momentum change flowing through a stenosis artery